# An Improved Force Field for $\mathbf{O}_{2}, \mathbf{C O}$ and $\mathbf{C N}$ Binding to Metalloporphyrins 

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#### Abstract

Parametrization of a molecular-mechanics program to include terms specific for five- and six-coordinate transition metal complexes is applied to heme complexes. The principal new feature peculiar to five and six coordination is a term that represents the effect of electron-pair repulsion modified by the ligand electronegativity and takes into account the different possible structures of complexes. The model system takes into account the structural differences of the fixing centre in the haemoglobin subunits. The customary proximal histidine is added. The macrocycle heme IX is wholly considered in our model. The calculations show clearly that certain conformations of heme IX-histidine models are much more favourable than others for fixing $\mathrm{O}_{2}$. From the $\mathrm{O}_{2}$ binding in haemoglobin and myoglobin and in simple Fe porphyrin models it is concluded that the bent $\mathrm{O}_{2}$ ligand is best viewed as bound superoxide, $\mathrm{O}_{2}^{-}$. Rotation of axial ligands are practically free. A small modification of the model in both crystal and protein matrix affects the orientation of the ligands in experimental systems.


Abbreviations: AM1 - Austin Model 1; CO - carbon monoxide; DFT - density functional theory; EPR - electronpair repulsion; Hb - haemoglobin; His - histidine; ID - interacting induced-dipole; Im - imidazole; LDA - local density approximation; Mb - myoglobin; mdi - malondialdiminate; MM - molecular mechanics; NID - non -interacting induced-dipole; $\mathrm{O}_{2}$ - oxygen; P - porphyrin; $\mathrm{Piv}_{2} \mathrm{C}_{8}-\alpha, \alpha, 5,15-\left[2,2^{\prime}\right.$-(octanediamido)diphenyl]$\alpha, \alpha, 10,20-$ bis(o-pivalamidophenyl)porphyrin; QM - quantum mechanics; TTP - meso-tetraphenylporphyrin.

## Introduction

The heme group is in the active centre of a number of relevant proteins as the oxygen $\left(\mathrm{O}_{2}\right)$ transport proteins haemoglobin $(\mathrm{Hb})$ and myoglobin $(\mathrm{Mb})$ [1, 2], as well as enzymes involved in catabolism as peroxidases [3], catalases, oxidases [4] and cytochromes [5]. The replacement of Fe by Mg in heme leads to chlorophyll [6], and the replacement of Fe by other transition metals coupled with modifications in the aromatic ring leads to species as vitamin $\mathrm{B}_{12}$ [7] and cofactor F-430 [8]. The study of heme models is a focal point of experimental bioinorganic chemistry [9].

Rohmer and co-workers characterized the electronic state of $\mathrm{Fe}(\mathrm{P})(\mathrm{P}=$ porphyrin $)$ complexes [10-12], and predicted an electronic structure, which was later proved by experiment [13]. Other theoretical studies are devoted to the real position of the CO group in $\mathrm{Fe}(\mathrm{P})(\mathrm{Im})(\mathrm{CO})(\mathrm{Im}=$ imidazole $)$ complexes [14, 15], the position of the CN group in $\mathrm{Fe}(\mathrm{mdi})_{2}(\mathrm{py})(\mathrm{CN})$ (mdi $=$ malondialdiminate) complexes [16], the role of histidine (His)-distal and -proximal on the binding of $\mathrm{O}_{2}$ in Hb [17-20], and structural aspects of the binding
of $\mathrm{O}_{2}$ and other ligands to heme [21-27]. The amount of information obtained from the quantum mechanical calculations is seriously limited by the size of the heme group itself, which has allowed only recently the appearance of theoretical studies on reactivity [28-33].

The coordination of $\mathrm{O}_{2}$ to the $\mathrm{Fe}(\mathrm{P})(\mathrm{Im})$ 5-coordinate species leads to 6 -coordinate species with octahedral geometry, i.e., the biomimetic forms of $\mathrm{Mb}-\mathrm{O}_{2}$ and $\mathrm{Hb}-\mathrm{O}_{2}$. X-ray data were reported only on two complexes, $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)[1-(\mathrm{Me}) \mathrm{Im}]\left(\mathrm{O}_{2}\right)[34]$ and $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)[2-$ ( Me ) Im$]\left(\mathrm{O}_{2}\right)$ [35]. Both complexes are quite similar, sharing the same porphyrin $\mathrm{T}_{\text {piv }} \mathrm{PP}$, which is mesotetrakis ( $\alpha, \alpha, \alpha, \alpha-o$-pivalamidophenyl)porphyrin. Maseras and co-workers optimized the geometry of $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)$ [1-(Me) Im$]\left(\mathrm{O}_{2}\right)$ with the hybrid quantum mechanics/ molecular mechanics (QM/MM) method IMOMM (DFT-B3LYP basis set double-ל(d):MM3) [36] and pure QM DFT-B3LYP basis set 6-31G(d) [37]. Ghosh and Bocian optimized the geometry of $\mathrm{Fe}(\mathrm{P})(\mathrm{Im})(\mathrm{CO})$ with density functional theory (DFT) basis set double$\zeta+$ polari-zation [19]. Salzmann et al. optimized under constraint the geometry of a $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)[1-(\mathrm{Me}) \mathrm{Im}](\mathrm{CO})$ model with DFT-B3LYP Watchers' 62111111/331211/

3111/3 basis set [38]. Han et al. calculated a heme modelCO system employing the ab initio pseudopotential method with local density approximation (LDA) exchange correlation (unpublished basis set) [39].

The reversible binding of $\mathrm{O}_{2}$ and carbon monoxide (CO) played a central role in studies of heme-protein structure and function. Numerous encumbered $\mathrm{Fe}^{\mathrm{II}}$ porphyrin models were synthesized in an effort to elucidate the structural details of small ligand binding. The steric bulk of certain axial ligands bonded to synthetic $\mathrm{Fe}^{\mathrm{II}}$ porphyrins provided model compounds of reduced $\mathrm{O}_{2}$ and CO affinity, and models of the socalled tense $(T)$ state of hemoproteins. Unfortunately, thus far there is only one single-crystal X-ray structure determination on such a complex [40]. There was much discussion on the mechanistic basis of the variation of affinity values in heme proteins and model compounds. This focused on the nature of the axial ligand, distal steric effects, distal polar effects, and enforced doming and ruffling of the porphyrin skeleton. Johansson et al. showed by quantum chemical calculations on a haem $a$ model that upon reduction the spin pairing at Fe is accompanied by effective delocalization of electrons from the Fe towards the periphery of the porphyrin ring, including its substituents [41, 42].

In previous papers [43, 44], both non-interacting (NID) and interacting (ID) induced-dipole polarization models were implemented in the program molecular mechanics (MM2) [45]. The polarizing force field for proteins (MMID2) was described elsewhere [43] and applied to $N$-formylglycinamide (For-Gly- $\mathrm{NH}_{2}$ ) [44]. MMID2 was improved to include terms specific for fiveand six-coordination [46]. The new program is called MMIDX. In this study a new force field for $\mathrm{O}_{2}, \mathrm{CO}$ and CN binding to metalloporphyrins has been tested. The next section presents the computational method. Following that, the improvements in the force field are described. Next, the calculation results are discussed. Finally, the conclusions are summarized.

## Computational method

The electric polarization energy $E^{\mathrm{pol}}$ is the energy required to make the induced dipoles,

$$
\begin{equation*}
E^{\mathrm{pol}}=\sum_{p=1}^{N} E_{p}^{\mathrm{pol}}=-\frac{1}{2} \sum_{p=1}^{N} \frac{\mu_{p} \cdot \mu_{p}}{\alpha_{p}} \tag{1}
\end{equation*}
$$

where $N$ is the number of atoms. The procedure by noninteracting induced dipoles (NID) assumes scalar isotropic point (atomic) polarizabilities. Since the electric field at each position must be evaluated to determine the induced dipoles, $E_{\mathrm{pol}}$ is most easily evaluated from this field,

$$
\begin{equation*}
E^{\mathrm{pol}}=-\frac{1}{2} \sum_{p=1}^{N} \alpha_{p} \mathbf{E}_{p} \cdot \mathbf{E}_{p} \tag{2}
\end{equation*}
$$

On the other hand, the procedure by interacting induced dipoles (ID) allows the interaction of the induced dipole moments by means of tensor effective anisotropic point polarizabilities. The molecular polarizability, $\alpha_{\alpha \beta}^{\mathrm{mol}}$, is defined as the linear response to an external field,

$$
\begin{equation*}
\mu_{\alpha}^{\mathrm{ind}}=\alpha_{\alpha \beta}^{\mathrm{mol}} E_{\beta}^{\mathrm{ext}} \tag{3}
\end{equation*}
$$

where $\mu_{\alpha}^{\text {ind }}$ is the induced molecular dipole moment. Considering a set of $N$ polarizable interacting atoms, the atomic induced dipole moment has a contribution also from the other atoms,

$$
\begin{equation*}
\mu_{p, \alpha}^{\mathrm{ind}}=\alpha_{p, \alpha \beta}\left(E_{\beta}^{\mathrm{ext}}+\sum_{q \neq p}^{N} T_{p q, \beta \gamma}^{(2)} \mu_{q, \gamma}^{\mathrm{ind}}\right), \tag{4}
\end{equation*}
$$

where $T_{p q, \beta \gamma}^{(2)}$ is the interaction tensor as modified by Thole [47]

$$
\begin{equation*}
T_{p q, \alpha \beta}^{(2)} \frac{3 v_{p q}^{4} r_{p q, \alpha} r_{p q, \beta}}{r_{p q}^{5}}-\frac{\left(4 v_{p q}^{3}-3 v_{p q}^{3}\right) \delta_{\alpha \beta}}{r_{p q}^{3}} \tag{5}
\end{equation*}
$$

where $v_{p q}=r_{p q} / s_{p q}$ if $r_{p q}<s_{p q}$; otherwise $v_{p q}=1 . s$ is defined as $\left(\Phi_{p} \Phi_{q}\right)^{1 / 4}$, where $\Phi_{p}$ is a fitting parameter proportional to the atomic second-order moment. Molecular polarizability can be written as

$$
\begin{equation*}
\alpha_{\alpha \beta}^{\mathrm{mol}}=\sum_{q, p}^{N} \mathbf{B}_{p q, \alpha \beta} \tag{6}
\end{equation*}
$$

where $\mathbf{B}$ is the relay matrix defined from atomic $\alpha$-s as (in a supermatrix notation)

$$
\begin{equation*}
\mathbf{B}=\left(\alpha^{-1}-T^{(2)}\right)^{-1} . \tag{7}
\end{equation*}
$$

## Force-field modifications

1,3-interactions between atoms bonded to a common atom are not specifically included in Equation (8) in the MM2 + polarization approach because they are effectively already included in the bond-length and bondangle strainless parameters.

$$
\begin{equation*}
E_{\text {steric }}=\sum E_{\text {str }}+\sum E_{\text {bend }}+\sum E_{\text {tors }}+\sum E_{\mathrm{nb}} \tag{8}
\end{equation*}
$$

However, for 5-coordinate structures, there is a need to consider the effect of 1,3-interactions because an energy term is needed for ligand-ligand repulsion to account for (1) the stability difference of various geometries possible, and (2) structural effects due to the variation of ligand electronegativity. Since the geometries of the methylfluorophosphoranes $\left(\mathrm{CH}_{3}\right)_{n} \mathrm{PF}_{5-n} \quad(n=0 \rightarrow 3)$ were qualitatively correlated with Gillespie's VSEPR theory, VSEPR was adopted as a model for the present
approach. Bond electron-pair repulsion (EPR) terms were introduced via the non-bonded term $E_{\mathrm{nb}}$ of Equation (6) modified to express EPR for atoms bonded to 5 - or 6-coordinated atoms. The unmodified term is

$$
\begin{equation*}
E_{\mathrm{nb}(A B)}=\varepsilon\left[8.28 \cdot 10^{5} \exp \left(-\frac{1}{0.0736 P}\right)-2.25 P^{6}\right], \tag{9}
\end{equation*}
$$

where $P=\left[r_{\mathrm{VDW}(A)}+r_{\mathrm{VDW}(B)}\right] / r_{A B}, r_{\mathrm{VDW}}$ is the van der Waals radius of the specific atom, and $r_{A B}$ is the nonbonded distance between $A$ and $B ; \varepsilon=\left(\varepsilon_{A} \varepsilon_{B}\right)^{1 / 2}$ where $\varepsilon_{A}$ and $\varepsilon_{B}$ are parameters specific to atoms $A$ and $B$, and are related to the hardness of the atoms. Hill evaluated the constants in Equation (9), which give the energy $E_{\mathrm{nb}(A B)}$ in units of kilocalories per mole [48].

The modification of Equation (7) to express 1,3-bond EPR terms is [49]

$$
\begin{equation*}
E_{(1,3) A B}=D \cdot \varepsilon\left[8.28 \cdot 10^{5} \exp \left(-\frac{1}{0.0736 P^{*}}\right)-2.25 P^{* 6}\right] . \tag{10}
\end{equation*}
$$

The addition of a scaling factor $D$, to obtain a suitable balance between this term and the other terms in Equation (6), and the replacement of $P$ with $P^{*}$ (where $P^{*}=\left[r_{\operatorname{VDW}(A)}+r_{\mathrm{VDW}(B)}\right] / r_{A B}^{*}$ and $r_{A B}^{*}$ is the distance between atoms $A$ and $B$ calculated from modified bond lengths, $d_{C A}^{*}$ and $d_{C B}^{*}$, between the central atom $C$ and either atom $A$ or $B$ ) provide the necessary adjustments to quantitatively reproduce the $\left(\mathrm{CH}_{3}\right)_{n} \mathrm{PF}_{5-n}$ structures [50]. The variation in ligand electronegativity is introduced by a distance factor $R_{A}$ in the relation $d_{C A}^{*}=d_{C A} R_{A}$. The magnitude of $R$ is inversely related to the electronegativity difference between atoms $C$ and $A$. The $R$ factors are the means of including the concept of EPR between atoms $A$ and $B$. If the electronegativity difference $\Delta X_{C A}$ is large, the bonding electron pair can be considered to move away from atom $C$, thus decreasing EPR between $C-A$ and $C-B$ bonds. When $\Delta X_{C A}>\Delta X_{C A^{\prime}}$, the repulsion term $E_{(1,3) A B}<E_{(1,3) A^{\prime} B}$ even when the actual bond lengths are equal. A set of distance factors $R$ may be obtained from the bond ionic character $I$,

$$
\begin{equation*}
I=1-\exp \left[-\frac{1}{4}\left(\Delta X_{C A}\right)^{2}\right] \tag{11}
\end{equation*}
$$

and using the relation

$$
\begin{equation*}
R=\frac{I \cdot r_{A}+r_{C}}{r_{A}+r_{C}} \tag{12}
\end{equation*}
$$

where $r_{A}$ and $r_{C}$ are covalent radii of atoms $A$ and $C$.

## Description of program POLAR

POLAR calculates molecular electric charges and polarizablities [51]. Describing the partial charge method developed for the Mulliken scale [52], Huheey men-
tioned that most elements double their electronegativities as the partial charge approaches +1 whereas their electronegativities essentially disappear as the partial charge approaches -1 [53]. The Mulliken and Pauling scales are roughly proportional, so Huheey's observation may be expressed in Pauling units as $X_{\text {eq }}=X_{A}+$ $\Delta_{A} X_{A}$. Here, $X_{\text {eq }}$ is the electronegativity as equalized through Sanderson's principle, $X_{A}$ is the initial, prebonded electronegativity of a particular atom $A$ and $\Delta_{A}$ is the $\sigma$ partial charge on $A$ [54]. Charge conservation leads to a general expression for $X_{\text {eq }}=(N+q) /\left(\Sigma_{\text {atoms }} v_{A} /\right.$ $X_{A}$ ), where $N=\Sigma v$ equals the total number of atoms in the species formula and $q$ is the $\sigma$ molecular charge. The $\sigma$ partial charge $\Delta_{A}$ on atom $A$ can be generalized as $\Delta_{A}=\Sigma_{\text {bonds }}\left(X_{\text {eq }, b}-X_{A}\right) / X_{A}$ and the electronegativity equalized for bonds is given as $X_{\text {eq }, b}=(2+q / m) /(1 /$ $X_{A}+1 / X_{B}$ ), where $m$ is the number of bonds in the molecule. $\pi$-net charges and polarizabilities have been evaluated with the Hückel molecular orbital (HMO) method. HMO $\beta$ parameter can be evaluated, in first approximation, between $p_{z}$ orbitals twisted from coplanarity by an angle $\theta$ as $\beta=\beta_{0} \cos \theta$, where $\beta_{0}$ is equal to the $\beta$ parameter for benzene [55]. The electronic coupling $V_{a b}$ of the binuclear mixed-valence $\mathrm{M}^{\mathrm{II}}-\mathrm{L}-\mathrm{M}^{\mathrm{III}}$ complex $\left.\left[\left(\mathrm{NH}_{3}\right)_{5} \text {-Ru-bipyridyl-Ru( } \mathrm{NH}_{3}\right)_{5}\right]^{5+}$ showed that when a pyridine ring rotates, $\pi-\pi V_{a b}(\theta)$ can be best fitted by $\cos ^{1.15} \theta$ [56]. The $\beta$ function is assumed universal:

$$
\begin{equation*}
\beta=\beta_{0} \cos ^{1.15} \theta \tag{13}
\end{equation*}
$$

The dipole and tensor quadrupole moments have been calculated from the point distribution of net charges. The dipole moment vector is calculated as

$$
\begin{equation*}
\mu_{a}=\sum_{i} q^{i} r_{a}^{i} \tag{14}
\end{equation*}
$$

where $q^{\mathrm{i}}$ is the $i$ th element of charge at the point $\mathbf{r}^{\mathrm{i}}$ relative to an origin fixed at the centre of mass. The subscripts $a, b, \ldots$, denote the Cartesian components. Only the first, nonvanishing moment is independent of the choice of origin. Thus for an ion like $\mathrm{OH}^{-}, \mu$ varies with the origin. In order to avoid this dependence, the origin is taken at the centre of mass and the molecule is brought into its principal internal coordinate system.

Sanderson's principle allows the calculation of the $\sigma$ atomic polarizability as:

$$
\begin{equation*}
\alpha_{A}=\frac{\partial \Delta_{A}}{\partial X_{A}}=\sum_{\text {bonds }} \frac{f_{A} s_{A}\left(1-\Delta_{A}\right)\left(2-\frac{q}{m}\right) X_{B}}{\left(2-\Delta_{A}-\Delta_{B}\right)\left(X_{A}+X_{B}\right)^{2}}, \tag{15}
\end{equation*}
$$

where the coefficients $f_{A}$ and $s_{A}$ have been introduced to take into account the effects of the atomic charge $\left(\Delta_{A}\right)$, internal sub-shells and lone pairs on $\alpha_{A} . f_{A}$ and $s_{A}$ are calculated as $f_{A}=1-1.5 \Delta_{A}+0.5 \Delta_{A}^{2}$ and $s_{A}=C_{A}+$ $0.15 L_{A}$, where $C_{A}$ is related to the number of internal sub-shells and $L_{\mathrm{A}}$ is the number of lone pairs on
atom $A$. The $\sigma$ atomic polarizability tensors are calculated as:

$$
\begin{align*}
\alpha_{\sigma} & =\sum_{\text {bonds }} \frac{3 \alpha_{\sigma}}{\alpha^{\|}+2 \alpha^{\perp}}\left[\begin{array}{ccc}
\alpha^{\perp} & 0 & 0 \\
0 & \alpha^{\perp} & 0 \\
0 & 0 & \alpha^{\|}
\end{array}\right] \\
& =\sum_{\text {bonds }} \frac{3 \alpha_{\sigma}}{3.676}\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1.676
\end{array}\right], \tag{16}
\end{align*}
$$

where the $z$-axis is along the bond direction for each bond. The diagonal form of $\alpha_{\sigma}$ has two components: $\alpha^{\|}$ and $\alpha^{\perp}$, parallel and perpendicular, respectively, to the bond axis. Parameter $\alpha^{\|} / \alpha^{\perp}=1.676$ has been obtained fitting the bonding polarizabilities of Vogel [57] implemented in the database of program SIBFA [58]. The $\pi$ atomic polarizability tensor is calculated as:

$$
\begin{align*}
\alpha_{\pi} & =\sum_{\text {bonds }} \frac{3 \alpha_{\pi}}{2 \alpha^{\|}+\alpha^{\perp}}\left[\begin{array}{ccc}
\alpha^{\|} & 0 & 0 \\
0 & \alpha^{\|} & 0 \\
0 & 0 & \alpha^{\perp}
\end{array}\right] \\
& =\sum_{\text {bonds }} \frac{3 \alpha_{\pi}}{3.741}\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1.741
\end{array}\right], \tag{17}
\end{align*}
$$

where the $x y$ plane is the $\sigma$-plane. $\alpha^{\|}$and $\alpha^{\perp}$ are parallel and perpendicular to the $\sigma$-plane. Parameter $\alpha^{\perp} /$ $\alpha^{\|}=1.741$ has been obtained by fitting the experimental polarizabilities of aromatic molecules.

## Calculation results and discussion

In a previous report [46] the MMX + polarization force field was applied to the binding of $\mathrm{O}_{2}, \mathrm{CO}$ and CN to
metalloporphyrins with an EPR parameter of $D=0.2$. In the present paper a comparative study is presented with $D=0.1$. The structure of the heme(-His) $-\mathrm{O}_{2}$ model is shown in Figure 1. Heme is the prosthetic group of Hb . The molecular mechanics calculations use the MM2/MMX + polarization force fields. The van der Waals parameters for the Fe atom have been taken from the UFF force field [59], and the torsional contributions involving dihedral angles with the metal atom and the bending terms involving Fe in central position have been set to zero.

The molecular mechanics dipole moment of the heme IX models is collected in Table 1. In general, the dipole moment increases with the oxidation state of Fe . In particular, the dipole moment of the $\mathrm{Fe}^{\mathrm{III}}$ heme (- $\mathrm{Hi}-$ s) -CN results the greatest due to the polar $\mathrm{Fe}^{\delta+}-\mathrm{C}-\mathrm{N}^{\delta-}$ complex. The dipole moment of the $\mathrm{Fe}^{\text {III }}$ heme $(-\mathrm{His})-\mathrm{O}_{2}$ is relatively large, due to the polar $\mathrm{Fe}^{\delta+}-\mathrm{O}-\mathrm{O}^{\delta-}$ complex. In general, the inclusion of polarization in MM2 corrects the dipole moment in the correct direction when compared with MMX + ID. In particular, for heme(-His) the MM2 + polarization dipole moment remains almost constant. The binding of His in heme increases the dipole moment by a factor of 6 . Moreover, the binding of CN in heme-His increases the dipole moment by $83 \%$. However, the binding of $\mathrm{O}_{2}$ or CO decreases the dipole moment by only $1-7 \%$.

## The 4-coordinate Fe (P) system

The heme group has little direct application in biochemistry, but it is a natural starting point for both experimental and theoretical studies. The crystal structures of a number of heme derivatives were reported, with different substituents in the ring [13]. The simplest


Figure 1. Stereo view of the heme $(-\mathrm{His})-\mathrm{O}_{2}$ model. Heme is the prosthetic group of haemoglobin.

Table 1. Molecular mechanics (MMX) results for heme-IX adduct models: dipole moments in debyes

| Adduct | Fe oxidation state | MM2 | $\mathrm{MM} 2+\mathrm{NID}^{\text {a }}$ | $\mathrm{MM} 2+\mathrm{ID}^{\text {b }}$ | MMX | $\mathrm{MMX}+\mathrm{NID}^{\text {a }}$ | MMX + $\mathrm{ID}^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Heme | 2 | 0.467 | 0.483 | 0.539 | 0.467 | 0.483 | 0.539 |
| Heme(-His) | 2 | 2.840 | 2.725 | 2.819 | 2.515 | 2.974 | 3.795 |
| Heme(-His)- $\mathrm{O}_{2}$ | 3 | 2.512 | 2.372 | 3.091 | 3.458 | 2.542 | 3.187 |
| Heme(-His)-CO | 2 | 2.723 | 2.725 | 2.905 | 3.252 | 1.878 | 2.567 |
| Heme(-His)-CN | 3 | 5.090 | 5.538 | 5.470 | 5.031 | 5.247 | 5.534 |

[^0]Table 2. Selected geometric parameters ( $\AA$ and degrees) from the geometry optimization of $\mathrm{Fe}(\mathrm{P})$ with the pure B3LYP and with the IMOMM(B3LYP:MM3) methods [37] ${ }^{\text {a }}$

| Parameter | MM2 | $\mathrm{MM} 2+\mathrm{NID}^{\text {b }}$ | $\mathrm{MM} 2+\mathrm{ID}^{\text {c }}$ | MMX ${ }^{\text {d }}$ | MMX ${ }^{\text {d }}+$ NID $^{\text {b }}$ | $\mathrm{MMX}^{\text {d }}+\mathrm{ID}^{\text {c }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Fe}-\mathrm{N}^{\mathrm{e}}$ | 1.881 | 1.878 | 1.877 | 1.881 | 1.878 | 1.877 |
| $\mathrm{N}-\mathrm{C}$ | 1.353 | 1.352 | 1.350 | 1.353 | 1.352 | 1.350 |
| $\mathrm{C}-\mathrm{C}_{\text {bridge }}$ | 1.337 | 1.336 | 1.334 | 1.337 | 1.336 | 1.334 |
| $\mathrm{C}-\mathrm{C}^{\prime}$ | 1.341 | 1.340 | 1.339 | 1.341 | 1.340 | 1.339 |
| $\mathrm{C}^{\prime}-\mathrm{C}^{\prime \prime}$ | 1.332 | 1.332 | 1.332 | 1.332 | 1.332 | 1.332 |
| $\mathrm{Fe}-\mathrm{N}-\mathrm{C}$ | 128.6 | 128.6 | 128.6 | 128.6 | 128.6 | 128.6 |
| $\mathrm{N}-\mathrm{Fe}-\mathrm{N}$ | 90.2 | 90.2 | 90.2 | 90.2 | 90.2 | 90.2 |
| $\mathrm{N}-\mathrm{C}-\mathrm{C}_{\text {bridge }}$ | 120.8 | 120.8 | 120.9 | 120.8 | 120.8 | 120.9 |
| $\mathrm{N}-\mathrm{C}-\mathrm{C}^{\prime}$ | 112.0 | 112.1 | 112.1 | 112.0 | 112.1 | 112.1 |
| Parameter | Experiment | Pure QM | QM/MM |  |  |  |
| $\mathrm{Fe}-\mathrm{N}$ | 1.966 | 2.016 | 1.940 |  |  |  |
| $\mathrm{N}-\mathrm{C}$ | $1.378{ }^{\text {e }}$ | 1.397 | 1.362 |  |  |  |
| $\mathrm{C}-\mathrm{C}_{\text {bridge }}$ | $1.395{ }^{\text {e }}$ | 1.402 | 1.369 |  |  |  |
| $\mathrm{C}-\mathrm{C}^{\prime}$ | $1.439^{\text {e }}$ | 1.459 | 1.345 |  |  |  |
| $\mathrm{C}^{\prime}-\mathrm{C}^{\prime \prime}$ | $1.365^{\text {e }}$ | 1.367 | 1.333 |  |  |  |
| $\mathrm{Fe}-\mathrm{N}-\mathrm{C}$ | $127.2{ }^{\text {e }}$ | 127.4 | 127.7 |  |  |  |
| $\mathrm{N}-\mathrm{Fe}-\mathrm{N}$ | $90.0{ }^{\text {e }}$ | 90.0 | 90.0 |  |  |  |
| $\mathrm{N}-\mathrm{C}-\mathrm{C}_{\text {bridge }}$ | $125.3{ }^{\text {e }}$ | 125.5 | 126.2 |  |  |  |
| $\mathrm{N}-\mathrm{C}-\mathrm{C}^{\prime}$ | $110.6^{\text {e }}$ | 110.4 | 110.3 |  |  |  |

${ }^{a}$ Experimental data on the Fe(TPP) system are also provided for comparison [13]; ${ }^{\mathrm{b}}$ NID: polarization by non-interacting induced dipoles; ${ }^{\mathrm{c}}$ ID: polarization by interacting induced dipoles; ${ }^{\mathrm{d}}$ Scaling factor $D=0.1$; ${ }^{\mathrm{e}}$ Average values.
model, with all substituents being H atoms, was not provided. Because of this, comparison will be made with a species containing some substituents. In particular, $\mathrm{Fe}(\mathrm{TPP})$ (TPP $=$ meso-tetraphenylporphyrin) has been chosen [13]. Its electronic state is well known experimentally to correspond to a low spin triplet $(S=1)$. Selected structural parameters are collected in Table 2. The agreement in bond angles between both MM2/ MMX + polarization geometries and the X-ray structure is good, with discrepancies always smaller than $5^{\circ}$. Differences in bond distances are larger in a number of cases. This is the case of the $\mathrm{C}-\mathrm{C}_{\text {bridge }}, \mathrm{C}-\mathrm{C}^{\prime}$ and $\mathrm{C}^{\prime}-\mathrm{C}^{\prime \prime}$ distances. These distances have values of 1.395, 1.439 and $1.365 \AA$, respectively, in X-ray, ca. 1.336, 1.340 and $1.332 \AA$, respectively, in MM2/MMX + popolarization. Agreement between experiment and MM2/MMX + polarization is good (ca. $0.06 \AA$ ). All these atoms are in part purely described with MM2, and the optimized MM2/MMX + polarization values are close to the optimal bond distance for these types of atoms in the applied force field, which is $1.337 \AA$. Another discrepancy in the geometries appears in the $\mathrm{Fe}-\mathrm{N}$ distance. This is more puzzling, because the calculated distance $1.877-1.881 \AA$ is smaller than the experimental value of $1.966 \AA$.

## The 5-coordinate $F e(P)$ (Im) system

Coordination of an Im ligand to the heme group leads to a 5-coordinate species with a square pyramidal geometry. These compounds are good biomimetic models of both Mb and Hb , Im replacing His-proximal of the biological systems. The need to avoid both dimerization
and formation of 6 -coordinate species with two axial ligands poses serious restrictions on the nature of the porphyrins able to give this kind of complexes. For this study, the species $\mathrm{Fe}\left(\mathrm{Piv}_{2} \mathrm{C}_{8}\right)[1-(\mathrm{Me}) \mathrm{Im}]\left\{\mathrm{Piv}_{2} \mathrm{C}_{8}=\right.$ $\alpha, \alpha, 5,15-\left[2,2^{\prime}\right.$-(octanediamido)diphenyl]- $\alpha, \alpha, 10,20-$ bis ( $o$ pivalamidophenyl)porphyrin\} has been chosen. This species has the advantage of having 1 -methylimidazole as axial ligand, in constrast with the more common 2methylimidazole, which is more sterically demanding. Unfortunately, neither for $\mathrm{Fe}\left(\mathrm{Piv}_{2} \mathrm{C}_{8}\right)$ [1-(Me)Im] nor for other 5 -coordinate derivatives of heme the electronic state is experimentally known. Electronic spectroscopy, magnetic susceptibility and Mössbauer measurements are conclusive in identifying it as high spin $(S=2)$. Selected parameters are resumed in Table 3. The $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$ distances are longer by ca. $0.05 \AA$ (MMX + ID) than those in the 4 -coordinate system. This trend is in agreement with the reference values. The result is fully consistent with the shift from low spin to high spin in the metal. The present result improves the previous study [46], which presented these distances longer by $0.06 \AA$. Most data focus on the description of Im. Overall agreement in the geometric parameters is correct. Moreover, one has to take with suspicion the Xray parameters of Im , which would make the $\mathrm{N}=\mathrm{C}$ double bond $\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\mathrm{Im}}$ of $\operatorname{Im}$ longer than the $\mathrm{N}-\mathrm{C}$ single bond $\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\mathrm{Im}}^{\prime}$. However the MM calculations are, in general, in agreement with the $\mathrm{QM} / \mathrm{MM}$ reference, which provides the expected result.

The sharper discrepancy concerns the $\mathrm{N}_{\text {porphy }}$ rin $-\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\mathrm{Im}}$ dihedral angle. This angle measures the rotation around the $\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}$ single bond, and rules the placement of the Im plane with respect to the

Table 3. Selected geometric parameters ( $\AA$ and degrees) from the geometry optimization of $\mathrm{Fe}(\mathrm{P})\left(\mathrm{NH}=\mathrm{CH}_{2}\right)$ with the pure B3LYP and of $\mathrm{Fe}(\mathrm{P})[1-(\mathrm{Me}) \mathrm{Im}]$ with the IMOMM(B3LYP:MM3) methods [37] ${ }^{\text {a }}$

| Parameter | MM2 | $\mathrm{MM} 2+\mathrm{NID}^{\text {b }}$ | $\mathrm{MM} 2+\mathrm{ID}^{\text {c }}$ | MMX ${ }^{\text {d }}$ | MMX ${ }^{\text {d }}+\mathrm{NID}^{\text {b }}$ | MMX ${ }^{\text {d }}+\mathrm{ID}^{\text {c }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}^{\mathrm{e}}$ | 1.897 | 1.894 | 1.890 | 1.921 | 1.904 | 1.923 |
| $\mathrm{Fe}-\mathrm{N}_{\text {Im }}$ | 1.866 | 1.863 | 1.864 | 2.003 | 1.936 | 2.015 |
| $\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\text {Im }}$ | 1.327 | 1.327 | 1.326 | 1.438 | 1.449 | 1.436 |
| $\mathrm{N}_{\mathrm{Im}}-\mathrm{C}^{\prime}{ }_{\text {Im }}$ | 1.344 | 1.343 | 1.338 | 1.464 | 1.442 | 1.412 |
| $\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\text {Im }}$ | 126.3 | 126.3 | 126.1 | 122.1 | 143.7 | 151.0 |
| $\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\mathrm{Im}}^{\prime}$ | 126.7 | 126.6 | 126.3 | 142.2 | 112.5 | 122.4 |
| $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\mathrm{Im}}$ | 115.8 | 115.7 | 114.9 | 162.0 | 103.5 | 138.4 |
| Parameter | Experiment |  | Pure QM |  | QM/MM |  |
| $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$ | 2.074 |  | 2.101 |  | 2.029 |  |
| $\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}$ | 2.134 |  | 2.252 |  | 2.233 |  |
| $\mathrm{N}_{\text {Im }}-\mathrm{C}_{\text {Im }}$ | 1.350 |  | 1.279 |  | 1.299 |  |
| $\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\text {Im }}^{\prime}$ | 1.250 |  | $-^{\text {f }}$ |  | $1.414^{\text {g }}$ |  |
| $\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\text {Im }}$ | 127.0 |  | 126.1 |  | 136.8 |  |
| $\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\mathrm{Im}}^{\prime}$ | 120.0 |  | 120.6 |  | 122.6 |  |
| $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\text {Im }}$ | 126.0 |  | 90.0 |  | 133.2 |  |

${ }^{\text {a }}$ Experimental data on the $\mathrm{Fe}\left(\mathrm{Piv}_{2} \mathrm{C}_{8}\right)[1-(\mathrm{Me}) \mathrm{Im}]$ system are also provided for comparison [60]; ${ }^{\mathrm{b}}$ NID: polarization by non-interacting induced dipoles; ${ }^{\mathrm{c}}$ ID: polarization by interacting induced dipoles; ${ }^{\mathrm{d}}$ Scaling factor $D=0.1 ;{ }^{\mathrm{e}}$ Average values; ${ }^{\mathrm{f}}$ Frozen in calculation; ${ }^{\mathrm{g}}$ Corresponds to $\mathrm{N}-\mathrm{H}$ in this calculation.
porphyrin ring. Its sign is arbitrary because the $x$ and $y$ directions are equivalent in absence of axial ligand. In this work, a positive sign has been chosen for consistence with data on the 6-coordinate complexes presented below. An angle of $90^{\circ}$ (like in the pure QM reference) means that the Im plane is eclipsing one of the $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$ bonds, while an angle of $135^{\circ}\left(\approx 133.2^{\circ}\right.$ in $\mathrm{QM} / \mathrm{MM}$ ) indicates a staggered orientation of Im with respect to the $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$ bonds. Therefore, both pure QM and $\mathrm{QM} / \mathrm{MM}$ values are just opposite with the experimental value ( $126.0^{\circ}$ ) lying in between, although closer to the $\mathrm{QM} / \mathrm{MM}$ value. The structural minima lead to structures where the Im ligand is located about the bisector of an angle $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$. The MMX + polarization results lie, in general, in the range $90^{\circ}-133^{\circ}$ of the references. The importance of the large discrepancy between different values is, however, arguable, because there is also a large dispersion in different experimental 5-coordinate derivatives of heme, as well as in experimental reports of both Mb and Hb . It seems, therefore, that the rotation around this single bond has a very low barrier.

## The 6-coordinate $\mathrm{Fe}(\mathrm{P})(\mathrm{Im})\left(\mathrm{O}_{2}\right)$ system

Coordination of $\mathrm{O}_{2}$ to the 5-coordinate heme-His species leads to 6 -coordinate species with an octahedral geometry. These compounds are the biomimetic forms of $\mathrm{Mb}-\mathrm{O}_{2}$ and $\mathrm{Hb}-\mathrm{O}_{2}$. X-ray data are reported only on two complexes, $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)[1-(\mathrm{Me}) \mathrm{Im}]\left(\mathrm{O}_{2}\right)$ and $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)[2-(\mathrm{Me}) \mathrm{Im}]\left(\mathrm{O}_{2}\right)$. Both complexes are quite similar, sharing the same porphyrin $\mathrm{T}_{\text {piv }} \mathrm{PP}$, which is meso-tetrakis $(\alpha, \alpha, \alpha, \alpha$-o-pivalamidophenyl)porphyrin. The $\mathrm{Fe}\left(\mathrm{T}_{\mathrm{piv}} \mathrm{PP}\right)[1-(\mathrm{Me}) \mathrm{Im}]\left(\mathrm{O}_{2}\right)$ complex, containing the less sterically demanding 1-methylimidazole ligand, has
been chosen for comparison. The state of this system is a low spin open-shell singlet $(S=1)$ resulting in a $\mathrm{Fe}^{\mathrm{III}}-\mathrm{O}_{2}^{-}$charge distribution. Selected parameters are reported in Table 4. The parameters concerning the coordination of $\mathrm{O}_{2}$, which are probably the most critical for the biochemical activity of Hb , are well reproduced. The computed values for the $\mathrm{Fe}-\mathrm{O}$ distance, 1.8-1.9 $\AA$, are close to the experimental value of $1.746 \AA$. The calculated values ( $1.21-1.30 \AA$ ) for the O-O distance are far from the experimental report of $1.163 \AA$. However, the experimental value (even shorter than the $1.21 \AA$ for free $\mathrm{O}_{2}$ ) is suspect, because of the disorder on the placement of the second O atom within the crystal, as admitted by the authors of the X-ray experiment themselves [34]. The $\mathrm{O}-\mathrm{O}$ interatomic distance increases from $1.21 \AA$ in free $\mathrm{O}_{2}$ to $1.298 \AA$ (MMX + ID), suggesting that electronic charge is transferred from FeP to $\mathrm{O}_{2}$, in agreement with the experimental result that the $\mathrm{Fe}-\mathrm{O}_{2}$ bond can be formally described as $\mathrm{Fe}^{\mathrm{III}}-\mathrm{O}_{2}^{-}$[9].

The most significant feature of the present structure is the bent $\mathrm{Fe}-\mathrm{O}-\mathrm{O}$ bond. The $\mathrm{Fe}-\mathrm{O}-\mathrm{O}$ bond angles are in all cases indicative of a bent $\eta^{1}$ coordination mode, where only one O atom is directly attached to the metal. These calculations are in agreement with the experiment and calculation references. Atomic net charges have been calculated with our program POLAR. The results, $q_{\mathrm{Fe}}=3.078, q_{\mathrm{O}(\mathrm{Fe})}=-0.412$ and $q_{\mathrm{O}(\mathrm{O})}=-0.531 \mathrm{e}$ are in agreement with Weiss' model for the $\mathrm{Fe}-\mathrm{O}_{2}$ bond in which the bond might be ionic between $\mathrm{ae}^{3+}$ and a superoxide ion, net charge being transferred from Fe to $\mathrm{O}_{2}\left(\mathrm{Fe}^{3+} \mathrm{O}_{2}^{-}\right)$[61]. Experimental support for Weiss' model was first advanced by Misra and Fridovich [62]. The geometry agrees with Pauling's prediction of a bent $\mathrm{FeO}_{2}$ bond, and the $\mathrm{O}-\mathrm{O}$ distance

Table 4. Selected geometric parameters ( $\AA$ and degrees) from the geometry optimization of $\mathrm{Fe}(\mathrm{P})\left(\mathrm{NH}=\mathrm{CH}_{2}\right)\left(\mathrm{O}_{2}\right)$ with the pure B3LYP and of $\mathrm{Fe}(\mathrm{P})[1-(\mathrm{Me}) \mathrm{Im}]\left(\mathrm{O}_{2}\right)$ with the IMOMM(B3LYP:MM3) methods [37], and of $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)(\mathrm{Im})\left(\mathrm{O}_{2}\right)$ with LSD [21] ${ }^{\text {a }}$

| Parameter | MM2 | $\mathrm{MM} 2+\mathrm{NID}^{\text {b }}$ | $\mathrm{MM} 2+\mathrm{ID}^{\mathrm{c}}$ | MMX ${ }^{\text {d }}$ | $\mathrm{MMX}^{\text {d }}+\mathrm{NID}^{\text {b }}$ | $\mathrm{MMX}^{\text {d }}+\mathrm{ID}^{\text {c }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}^{\mathrm{e}}$ | 1.880 | 1.876 | 1.870 | 1.923 | 1.925 | 1.909 |
| $\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}$ | 1.871 | 1.862 | 1.861 | 2.020 | 1.990 | 1.996 |
| $\mathrm{Fe}-\mathrm{O}$ | 1.847 | 1.841 | 1.845 | 1.890 | 1.875 | 1.910 |
| $\mathrm{O}-\mathrm{O}$ | 1.211 | 1.210 | 1.210 | 1.279 | 1.269 | 1.298 |
| $\mathrm{Fe}-\mathrm{O}-\mathrm{O}$ | 123.5 | 121.5 | 122.8 | 120.1 | 143.9 | 125.8 |
| $\mathrm{O}-\mathrm{Fe}-\mathrm{N}_{\text {Im }}$ | 171.7 | 169.5 | 168.6 | 139.1 | 129.0 | 136.5 |
| $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\mathrm{Im}}$ | 179.0 | 178.2 | 176.8 | 170.4 | 170.2 | 173.4 |
| $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{O}-\mathrm{O}$ | -3.3 | -5.0 | -16.5 | -36.7 | -29.0 | -21.1 |
| Parameter | Experiment | Pure QM |  | QM/MM |  | LSD |
| $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$ | 1.978 | 2.035 |  | 1.949 |  | 2.010 |
| $\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}$ | 2.070 | 2.050 |  | 2.167 |  | $2.070^{\text {f }}$ |
| $\mathrm{Fe}-\mathrm{O}$ | 1.746 | 1.757 |  | 1.759 |  | 1.770 |
| $\mathrm{O}-\mathrm{O}$ | 1.163 | 1.268 |  | 1.286 |  | 1.300 |
| $\mathrm{Fe}-\mathrm{O}-\mathrm{O}$ | 129.4 | 121.1 |  | 117.0 |  | 121.0 |
| $\mathrm{O}-\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}$ | 180.0 | 175.8 |  | 179.4 |  | - |
| $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\text {Im }}$ | 159.5 | 177.9 |  | 137.0 |  | - |
| $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{O}-\mathrm{O}$ | -42.4 | -44.6 |  | -44.1 |  | - |

${ }^{\text {a }}$ Experimental data on the $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)[1-(\mathrm{Me}) \mathrm{Im}]\left(\mathrm{O}_{2}\right)$ system are also provided for comparison [34]; ${ }^{\text {b }}$ NID: polarization by non-interacting induced dipoles; ${ }^{\mathrm{c}}$ ID: polarization by interacting induced dipoles; ${ }^{\mathrm{d}}$ Scaling factor $D=0.1 ;{ }^{\mathrm{e}}$ Average values; ${ }^{\mathrm{f}}$ Frozen in calculation.
is close to that of $1.27 \AA$, predicted by him [63]. It is slightly shorter than that of $1.34 \AA$ in $\mathrm{O}_{2}^{-}$, close to the electron spin resonance results, which show that no more than $2 / 3$ of the density of one electron is transferred from the metal to the antibonding $\pi^{*}$ orbitals of $\mathrm{O}_{2}$.

The sharper discrepancy concerns the $\mathrm{N}_{\text {porphyrin }}$ -$\mathrm{Fe}-\mathrm{O}-\mathrm{O}$ dihedral angle. This angle measures the rotation around the $\mathrm{Fe}-\mathrm{O}$ single bond, and rules the placement of the $\mathrm{Fe}-\mathrm{O}-\mathrm{O}$ plane with respect to the porphyrin ring. An angle of $0^{\circ}\left(\approx-3.3^{\circ}\right.$ in MM2) means that the $\mathrm{Fe}-\mathrm{O}-\mathrm{O}$ plane is eclipsing one of the $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$ bonds, while an angle of $-45^{\circ}\left(\approx-44.6^{\circ}\right.$ in pure QM ) indicates a staggered orientation of the $\mathrm{O}_{2}$ with respect to the $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$ bonds. The structural minima lead to structures where the $\mathrm{O}_{2}$ ligand is located about the bisector of an angle $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$. The MMX/MMX + NID results lie near the reference results. The present result (MMX + polarization mean angle of $-29^{\circ}$ ) improves the previous study (mean angle of $-24^{\circ}$ ) [46]. The structural minima correspond to a situation where the ending O of $\mathrm{O}_{2}$ is placed above the opposite quadrant where the $\mathrm{N}_{\mathrm{Im}}^{\prime}$ is placed. This corresponds to a trans isomer.

## The 6-coordinate $\mathrm{Fe}(P)(\mathrm{Im})(\mathrm{CO})$ system

Selected structural parameters of $\mathrm{Fe}(\mathrm{P})(\mathrm{Im})(\mathrm{CO})$ are shown in Table 5. The geometric parameters concerning the coordination of CO , which are probably the most critical for the biochemical activity of Hb , are well reproduced. The computed values for the $\mathrm{Fe}-\mathrm{C}$ dis-
tance, $2.0-2.1 \AA$, are close to the experimental value of $1.793 \AA$. The calculated values ( $1.1-1.2 \AA$ ) for the $\mathrm{C}-\mathrm{O}$ distance are close to the experimental report of $1.095 \AA$. The $\mathrm{C}-\mathrm{O}$ interatomic distance is similar in the free molecule ( $1.171 \AA$, calculated with AM1 [64]) and $1.169 \AA$ (MMX), suggesting that electronic charge is not transferred from FeP to CO . This is in agreement with the experimental result that the $\mathrm{Fe}-\mathrm{CO}$ bond can be formally described as $\mathrm{Fe}^{\mathrm{II}}-\mathrm{CO}$ [9].

The most significant feature of the present structure is the linear $\mathrm{Fe}-\mathrm{C}-\mathrm{O}$ bond. While such a linear bond is to be expected based on the extensive literature on transition metal CO complexes, the result is nonetheless highly significant since bent $\mathrm{Fe}-\mathrm{C}-\mathrm{O}$ bonds with bond angles of $135^{\circ}-145^{\circ}$ appear to be the rule in various CO complexes of hemoproteins [65-67]. The global energy minimum is linear for $\mathrm{Fe}-\mathrm{C}-\mathrm{O}$ (MM2 + polarization, MMX and MMX + ID). These calculations are in agreement with the experiment and calculation references.

The rotation of the Im side chain is significant. The Im ring is rotated so that the N atom is directed toward the Fe atom, and the rotation angle $\mathrm{N}_{\text {porphyrin }}$ -$\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}-\mathrm{C}_{\mathrm{Im}}$ reaches ca. $176^{\circ}$ (MM2 + polarization) in agreement with the LDA reference $\left(174.2^{\circ}\right)$. The present result (MMX + polarization mean angle of $172^{\circ}$ ) improves the previous study (mean angle of $155^{\circ}$ (46].

## The 6-coordinate $\operatorname{Fe}(P)(\operatorname{Im})(C N)$ system

Selected bond lengths and angles are summarized in Table 6. The geometric parameters concerning the coor-

Table 5. Selected geometric parameters ( $\AA$ and degrees) from the complete geometry optimization of $\mathrm{Fe}(\mathrm{P})(\mathrm{Im})(\mathrm{CO})$ with LDA [39], partial geometry optimization of $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)[1-(\mathrm{Me}) \mathrm{Im}](\mathrm{CO})$ with DFT (B3LYP and BPW91) [38], and complete geometry optimization of $\mathrm{Fe}(\mathrm{mdi})_{2}(\mathrm{py})(\mathrm{CO})$ with NLDFT [16], of $\mathrm{Fe}(\mathrm{P})(\mathrm{Im})(\mathrm{CO})$ with LDFT [19] and of $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)(\mathrm{Im})(\mathrm{CO})$ with LSD [21] ${ }^{\text {a }}$

| Parameter | MM2 | $\mathrm{MM} 2+\mathrm{NID}^{\text {b }}$ | $\mathrm{MM} 2+\mathrm{ID}^{\mathrm{c}}$ | MMX ${ }^{\text {d }}$ | MMX ${ }^{\text {d }}+$ NID $^{\text {b }}$ |  | MMX ${ }^{\text {d }}+\mathrm{ID}^{\text {c }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}^{\mathrm{e}}$ | 1.878 | 1.873 | 1.871 | 1.888 | 1.917 |  | 1.896 |
| $\mathrm{Fe}-\mathrm{N}_{\text {Im }}$ | 1.868 | 1.863 | 1.862 | 1.947 | 2.043 |  | 1.977 |
| $\mathrm{Fe}-\mathrm{C}$ | 1.971 | 1.970 | 1.970 | 2.050 | 2.118 |  | 2.048 |
| $\mathrm{C}-\mathrm{O}$ | 1.110 | 1.109 | 1.110 | 1.169 | 1.166 |  | 1.166 |
| $\mathrm{Fe}-\mathrm{C}-\mathrm{O}$ | 180.0 | 180.0 | 180.0 | 176.1 | 167.9 |  | 176.9 |
| $\mathrm{C}-\mathrm{Fe}-\mathrm{N}_{\text {Im }}$ | 179.7 | 174.6 | 174.3 | 135.6 | 127.2 |  | 136.4 |
| $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{N}_{\text {Im }}-\mathrm{C}_{\text {Im }}$ | 136.0 | 178.9 | 176.0 | 178.3 | 177.8 |  | 159.1 |
| Parameter | Experiment | LDA | B3LYP | BPW91 | NLDFT | LDFT | LSD |
| $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$ | 2.003 | 1.990 | - | - | 1.961 | 1.983 | 2.020 |
| $\mathrm{Fe}-\mathrm{N}_{\text {Im }}$ | 2.071 | 1.960 | - | - | 2.139 | 1.966 | $2.070^{\text {f }}$ |
| $\mathrm{Fe}-\mathrm{C}$ | 1.793 | 1.790 | 1.801 | 1.743 | 1.739 | 1.733 | 1.720 |
| $\mathrm{C}-\mathrm{O}$ | 1.095 | 1.160 | 1.147 | 1.167 | 1.166 | 1.165 | 1.170 |
| $\mathrm{Fe}-\mathrm{C}-\mathrm{O}$ | 179.3 | 180.0 | 180.0 | 180.0 | 180.0 | 180.0 | 180.0 |
| $\mathrm{C}-\mathrm{Fe}-\mathrm{N}_{\text {Im }}$ | 178.3 | 180.0 | 180.0 | 180.0 | 180.0 | 180.0 | - |
| $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{N}_{\text {Im }}-\mathrm{C}_{\text {Im }}$ | - | 174.2 | - | - | - | - | - |

${ }^{\text {a }}$ Experimental data on the $\mathrm{Fe}\left(\mathrm{T}_{\text {piv }} \mathrm{PP}\right)[1-(\mathrm{Me}) \mathrm{Im}](\mathrm{CO})$ system are also provided for comparison [38]; ${ }^{\mathrm{b}}$ NID: polarization by non-interacting induced dipoles; ${ }^{\mathrm{c}}$ ID: polarization by interacting induced dipoles; ${ }^{\mathrm{d}}$ Scaling factor $D=0.1 ;{ }^{\mathrm{e}}$ Average values; ${ }^{\mathrm{f}}$ Frozen in calculation.
dination of CN are well reproduced. The computed values for the $\mathrm{Fe}-\mathrm{C}$ distance, $1.9-2.1 \AA$, are in agreement with the experimental value of $1.930 \AA$. The calculated values $(1.16-1.22 \AA)$ for the $\mathrm{C}-\mathrm{N}$ distance are close from the experimental report of $1.150 \AA$. The $\mathrm{C}-\mathrm{N}$ interatomic distance increases from $1.147 \AA$ (AM1) in the free molecule to $1.217 \AA$ (MMX + NID), suggesting that electronic charge is transferred from FeP to CN . This is in agreement with the experimental result that the $\mathrm{Fe}-\mathrm{CN}$ bond can be formally described as $\mathrm{Fe}^{\mathrm{III}}-(\mathrm{CN})^{-}[9]$.

The most significant feature of the present structure is the linear $\mathrm{Fe}-\mathrm{C}-\mathrm{N}$ bond. The global energy minimum is linear for $\mathrm{Fe}-\mathrm{C}-\mathrm{N}$ (MM2/MMX + polarization). These calculations are in agreement with the experiment and calculation references and with the previous study [46].

## Conclusions

From the preceding results the following conclusions can be drawn.

1. For the heme-IX adducts, the non-interacting or interacting induced-dipole polarization energy represents $74 \%$ of the total energy MM2 + polarization. The electron-pair repulsion energy corresponds to $50 \%$ of the total energy MMX + polarization.
2. The model system takes into account the structural differences of the fixing centre in the Hb subunits. Certain conformations of heme IX-His models are much more favourable that others for fixing $\mathrm{O}_{2}$.
3. Three different models of Fe-binding are proposed for $\mathrm{O}_{2}, \mathrm{CO}$ and CN ligands: bent superoxide

Table 6. Selected geometric parameters ( $\AA$ and degrees) from the geometry optimization of $\mathrm{Fe}(\mathrm{mdi})_{2}(\mathrm{py})(\mathrm{CN})$ with NLDFT [16] ${ }^{\mathrm{a}}$

| Parameter | MM2 | $\mathrm{MM} 2+\mathrm{NID}^{\text {b }}$ | $\mathrm{MM} 2+\mathrm{ID}^{\text {c }}$ | MMX ${ }^{\text {d }}$ | MMX ${ }^{\text {d }}+$ NID $^{\text {b }}$ | MMX ${ }^{\text {d }}+\mathrm{ID}^{\text {c }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}{ }^{\text {e }}$ | 1.878 | 1.871 | 1.867 | 1.905 | 1.891 | 1.904 |
| $\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}$ | 1.868 | 1.860 | 1.858 | 2.022 | 1.964 | 2.036 |
| $\mathrm{Fe}-\mathrm{C}$ | 1.944 | 1.942 | 1.941 | 2.079 | 2.032 | 2.064 |
| $\mathrm{C}-\mathrm{N}$ | 1.164 | 1.163 | 1.164 | 1.211 | 1.217 | 1.216 |
| $\mathrm{Fe}-\mathrm{C}-\mathrm{N}$ | 179.8 | 179.8 | 179.6 | 176.2 | 177.1 | 177.3 |
| Parameter |  | Experiment |  |  | NLDFT |  |
| $\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$ |  | 1.980 |  |  | 1.917 |  |
| $\mathrm{Fe}-\mathrm{N}_{\mathrm{Im}}$ |  | 2.090 |  |  | 2.159 |  |
| $\mathrm{Fe}-\mathrm{C}$ |  | 1.930 |  |  | 1.903 |  |
| $\mathrm{C}-\mathrm{N}$ |  | 1.150 |  |  | 1.173 |  |
| $\mathrm{Fe}-\mathrm{C}-\mathrm{N}$ |  | 180.0 |  |  | 180.0 |  |

[^1]$\mathrm{Fe}^{\mathrm{III}}-\mathrm{O}_{2}^{-}$, linear $\mathrm{Fe}^{\mathrm{II}}-\mathrm{CO}$ and linear $\mathrm{Fe}^{\mathrm{III}}-\mathrm{CN}^{-}$. The nature of $\mathrm{O}_{2}$ binding in $\mathrm{Hb}, \mathrm{Mb}$ and simple $\mathrm{Fe}-$ porphyrin models is becoming clear. When $\mathrm{O}_{2}$ is bound as a bent, rather than a triangular, ligand, it is best described as bound superoxide. This bent geometry may be critical to biological functioning because it allows the discrimination between $\mathrm{O}_{2}$ and CO.
4. Rotations of Im and $\mathrm{O}_{2}$ axial ligands about their linkages with Fe are unexpensive for both 5- and 6coordinated systems. These rotations are practically free. A small modification of the model in both crystal and protein matrix affects the orientation of the ligands in experimental systems. In the structural minima the axial ligands are located about the bisector of an angle $\mathrm{N}_{\text {porphyrin }}-\mathrm{Fe}-\mathrm{N}_{\text {porphyrin }}$.
5. The fact that in the present structure, a close analogue of the CO complexes of the hemoproteins, the $\mathrm{Fe}-\mathrm{C}-\mathrm{O}$ linkage is linear strongly suggests that another interpretation of the results of the protein studies is in order. The allegedly bent $\mathrm{Fe}-\mathrm{C}-\mathrm{O}$ linkage in these proteins is derived from Fourier maps on which the C and O atoms remain unresolved. These maps were interpreted on the assumption that the $\mathrm{Fe}-\mathrm{C}$ vector is perpendicular to the porphyrin plane. It is much more reasonable to expect that owing to the fixed nature of the globin pocket bending will occur at the Fe atom, leading to a linear $\mathrm{Fe}-\mathrm{C}-\mathrm{O}$ bond, which is not perpendicular to the porphyrin plane.
6. The geometry optimizations performed on the experimental structures present a good agreement with the X-ray results, in spite of that only certain residues of the fixing centre have been taken into account. In oxy- Hb , His-distal is engaged in an H -bond with the O directly linked with Fe . The H-bond in the fixing centres of Hb differs from that customarily observed in the biomimetic systems and Mb , in which the H bond is formed with the ending O . The electronic density of $\mathrm{O}(\mathrm{Fe})$ is lower than that of $\mathrm{O}(\mathrm{O})$, suggesting that the H -bond between O and His-distal is weaker than in Mb.

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## Appendix A. Force-field parameters

The MM2 parameter set (1980) has been used. Additional parameters are listed in Table A1. Type 13 is used for Fe .

Table A1. Additional MM2 parameters (Type 13 is used for Fe )

| Angle | $V_{1}$ | $V_{2}$ | $V_{3}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Torsional |  |  |  |  |  |
| Parameters |  |  |  |  |  |
| 1-1-2-7 | -0.44 | 0.24 | 0.06 |  |  |
| 1-1-2-9 | -0.44 | 0.24 | 0.06 |  |  |
| 5-1-2-7 | 0.0 | 0.0 | -0.24 |  |  |
| 5-1-2-9 | 0.0 | 0.0 | -0.24 |  |  |
| 1-2-2-9 | 0.0 | 10.0 | 0.0 |  |  |
| 2-2-2-9 | 0.0 | 10.0 | 0.0 |  |  |
| 5-2-2-9 | 0.0 | 10.0 | 0.0 |  |  |
| 9-2-2-9 | 0.0 | 10.0 | 0.0 |  |  |
| 1-2-6-24 | 0.0 | 0.0 | 0.0 |  |  |
| 7-2-6-24 | 1.0 | 1.65 | 0.0 |  |  |
| 1-2-9-2 | 0.0 | 10.0 | 0.0 |  |  |
| 1-2-9-28 | 0.0 | 0.0 | 0.0 |  |  |
| 2-2-9-2 | 0.0 | 10.0 | 0.0 |  |  |
| 2-2-9-13 | 0.0 | 0.0 | 0.0 |  |  |
| 2-2-9-28 | 0.0 | 0.0 | 0.0 |  |  |
| 5-2-9-2 | 0.0 | 10.0 | 0.0 |  |  |
| 5-2-9-13 | 0.0 | 0.0 | 0.0 |  |  |
| 5-2-9-28 | 0.0 | 0.0 | 0.0 |  |  |
| 9-2-9-2 | 0.0 | 10.0 | 0.0 |  |  |
| 9-2-9-13 | 0.0 | 0.0 | 0.0 |  |  |
| 7-4-13-9 | 0.0 | 0.0 | 0.0 |  |  |
| 10-4-13-9 | 0.0 | 0.0 | 0.0 |  |  |
| 7-7-13-9 | 0.0 | 0.0 | 0.0 |  |  |
| 2-9-13-4 | 0.0 | 0.0 | 0.0 |  |  |
| 2-9-13-7 | 0.0 | 0.0 | 0.0 |  |  |
| 2-9-13-9 | 0.0 | 0.0 | 0.0 |  |  |
| Stretching parameters |  |  |  |  |  |
| Bond | $k_{1}$ | $l_{0}$ | $l_{1}$ | Bond moment | Fe oxidation state |
| 4-7 | 10.0 | 1.110 | 0.0 | 0.089 | 2 |
| 4-7 | 10.0 | 1.158 | 0.0 | 0.010 | 3 |
| 4-13 | 10.0 | 1.968 | 0.0 | -1.304 | 2 |
| 4-13 | 10.0 | 1.940 | 0.0 | -1.374 | 3 |
| 7-7 | 10.0 | 1.210 | 0.0 | 0.000 | 3 |
| 7-13 | 10.0 | 1.841 | 0.0 | -1.641 | 3 |
| 9-13 | 10.0 | 1.867 | 0.0 | -1.514 | 2,3 |
| Van der Waals parameters |  |  |  |  |  |
| Atom | Type | R* | EPS | At. wt. |  |
| 13 | Fe | 0.013 | 2.912 | 55.85 |  |
| Bending parameters |  |  |  |  |  |
| Angle | $k_{\theta}$ | $\theta_{0}$ |  |  |  |
| 1-2-7 | 0.5 | 120.0 |  |  |  |
| 1-2-9 | 0.5 | 126.0 |  |  |  |
| 2-2-9 | 0.5 | 108.0 |  |  |  |
| 5-2-9 | 0.5 | 126.0 |  |  |  |
| 6-2-7 | 0.5 | 120.0 |  |  |  |
| 7-4-13 | 0.5 | 180.0 |  |  |  |
| 10-4-13 | 0.5 | 180.0 |  |  |  |
| 2-6-24 | 0.5 | 109.47122 |  |  |  |
| 7-7-13 | 0.5 | 121.0 |  |  |  |
| 2-9-2 | 0.5 | 108.0 |  |  |  |
| 2-9-13 | 0.5 | 126.0 |  |  |  |
| 4-13-9 | 0.0 | 109.47122 |  |  |  |
| 7-13-9 | 0.0 | 109.47122 |  |  |  |
| 9-13-9 | 0.0 | 109.47122 |  |  |  |

Table A1. (Continued)

| Out-of-plane |  |  |
| :--- | :---: | :---: |
| Angle | $K_{\theta}$ | $\theta_{0}$ |
| $9-13$ | 0.05 | 0.0 |
| Stretching-bending |  |  |
| parameters |  |  |
| Parameter | $k_{1 \theta}$ |  |
| 1 | 0.0 |  |
| 2 | 0.0 |  |
| 3 | 0.0 |  |
| 4 | 0.0 |  |

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[^0]:    ${ }^{\text {a }}$ NID: polarization by non-interacting induced dipoles; ${ }^{\mathrm{b}}$ ID: polarization by interacting induced dipoles.

[^1]:    ${ }^{\mathrm{a}}$ Experimental data on the $[\mathrm{Fe}(\mathrm{OEP})(\mathrm{py})(\mathrm{CN})]$ system are also provided for comparison [68]; ${ }^{\mathrm{b}}$ NID: polarization by non-interacting induced dipoles; ${ }^{\mathrm{c}}$ ID: polarization by interacting induced dipoles; ${ }^{\mathrm{d}}$ Scaling factor $D=0.1$; ${ }^{\mathrm{e}}$ Average values.

